Typestate-Oriented Design
A Coloured Petri Net Approach

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Abstract
Typestate Oriented programming is an extension of the object-oriented paradigm, where objects are modeled in terms of changing states. This paper propose the use of coloured petri nets as technique of design typestates for Typestate Oriented Programming.

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1. Introduction
Typestate-oriented programming [1] is a novel approach where objects are modeled in terms of changing states, this approach allows that each state may have its own representation and methods which may transition the object into a new state.

Petri nets are a powerful modelling technique for systems, Petri nets originate from the early work of Carl Adam Petri[8]. Coloured Petri nets [7] are an extension to basic petri nets that make them more useful for practical modelling.

The current design of the typestates[1] is made with simple state machines (Petri nets are more sophisticated state machines). This work propose the use of non-hierarchical petri nets to design typestates for typestate oriented programming.

This paper is organized as follows: Section 2 briefly reviews typestate, typestates for objects and typestate oriented programming concepts. Section 3 describe two petri nets concepts such place/transition nets and non hierarchical coloured petri nets, this section gives an example to understand the concepts. Section 4 show how use non-hierarchical coloured petri nets to design typestates for typestate oriented programming, this section shows three examples: iterator, graphical user interface and files.

2. Typestate: A programming language concept
2.1 Typestates for Objects
Typestate [9] is a refinement of concept of type of the data object, while type of the data object determines the set of operations ever permitted on the object, typestate determine the subset of these operations which is permitted in particular context and captures the notion of an objects begin in appropriate or inappropriate state for the application of a particular operation.

Each type has an associated set of typestates. An object of a given type is at each point in a program in a single one of the typestates associated with its type. In each typestate, it is legal to apply some operations of the type, but not others.

The typestate transition is defined by a typestate precondition, which may hold in order for the operation to be applicable, and one or more typestate postcondition reflection the possible typestates of the operand after the operation is applied.

Objects change state over time. providing the programmer with logic for writing precondition, postcondition, and objects invariants quickly run into decidability problems [4]. Typestates capture aspects of the state of an object, when an objects state changes its typestate may change as well.

2.2 Typestate Oriented Programming
Typestate Oriented Programming [1] is a new paradigm that extends object-oriented programming with typestates. Plaid [10] is a new programming language designed to support Typestate oriented Programming (Figure 1). In this approach a typestate is like a class in that it has its own interface (a set of method signatures), representation (fields), and behavior (method implementations).

Characteristics of Typestate Oriented Programming:
• The programs are made up of dynamically created objects,
• Each object has a typestate that is changeable.
• Each typestate has an interface, representation, and behavior.

As an example consider the Figure 1. A File can have different states, for example closeFile or openFile. This approach is different from object oriented programming in the sense that an object has encapsulated all behavior. State of a file can change, for example a closedFile can be open (state of the file is now openFile) file, this natural behavior is syntactically represented in PLAID as [ClosedFile >> OpenFile].

3. Petri Nets
3.1 Place/Transition Nets
Petri Nets also called Place/Transition Nets (PT-nets), are used for many different practical purposes, they have a graphical represen-
tation and a well-defined semantics allowing formal analysis. They are useful for modelling concurrent, distributed, asynchronous behavior in a system.

A net is a bipartite graph $G(V, E)$ where:

- $V = P \cup T$, $P$ is the set of places represented with circles and $T$ is the set of transitions represented with vertical bars.

**Definition** A PT-net is a tuple $\text{PTN} = \{P, T, A, W, M_0\}$ satisfying the requirements below:

- $P$ is a finite set of places
- $T$ is a finite set of transitions
- $A \subseteq (P \times T) \cup (T \times P)$ is a finite set of arcs
- $W : A \rightarrow \{1, 2, 3, \ldots\}$ is a weighting function
- $M_0 : P \rightarrow \{1, 2, 3, \ldots\}$ is the initial marking
- $(P \cap T) = \phi$ and $(P \cup T) = \phi$

A transition $t \in T$ is enabled if there is a token in each $p \in P$ that has and edge to the transition. An enabled transition may or may not occur (Figure 2).

### 3.2 Non-hierarchical CP-net

A PT-net has no types and no modules, with Coloured Petri Nets (CP-nets) it is possible to use data types and complex manipulation. CP-nets are a extension of Petri Nets where each token has attached a data value called the token colour, the token colours can be manipulated by the occurring transitions. With CP-nets it is possible to make hierarchical descriptions (hierarchical CP-nets) for example a large model can be obtained by combining a set of sub-models. Hierarchical CPN-nets allow well-defined interfaces between sub-models, well-defined semantics of the combined model and also sub-models can be reused.

### 3.3 Definition of non-hierarchical CP-nets: [7]

**Definition** A non-hierarchical CP-net is a tuple $\text{CPN} = \{\Sigma, P, T, A, N, C, G, E, I\}$ satisfying the requirements below:

1. $\Sigma$ is a finite set of non-empty types, called **colour set**.
2. $P$ is a finite set of **places**.
3. $T$ is a finite set of **transitions**.
4. $A$ is a finite set of **arcs** such that:
   \[ P \cap T = P \cap A = T \cap A = \phi \]
5. $N$ is a **node** function. It is defined from $A$ into $T \times T \cup T \times P$.
6. $C$ is a **colour** function. It is defined from $P$ into $\Sigma$.
7. $G$ is a **guard** function. It is defined from $T$ into expressions such that:
   \[ \forall t \in T : [\text{Type}(G(t)) = \text{Boolean} \land \text{Type}(\text{Var}(G(t))) \subseteq \Sigma] \]
8. $E$ is an **arc expression** function. It is defined from $A$ into expressions such that:
   \[ \forall a \in A : [\text{Type}(E(a)) = C(p(a)) \land \text{Type}(\text{Var}(E(a))) \subseteq \Sigma], where p(a) is the place of N(a) \]
9. $I$ is the **initialization** function. It is defined from $P$ into closed expressions such that:
   \[ \forall p \in P : [\text{Type}(I(p)) = C(p) \land p(a) \]

As a example consider a CPN-net from Figure 3. The **colour sets** determines the types, operations and functions that can be used in the net inscriptions i.e., arc expressions, guards, initialization expressions, etc. In the example:

- $\Sigma = \{U, I, P, E\}$.

The **places**, **transitions** and **arcs** are described by three sets $P$, $T$ and $A$. In the example:

- $P = \{A, B, C, D, E, R, S, T\}$
- $T = \{T_1, T_2, T_3, T_4, T_5\}$
- $A = \{(A, T_1), (T_1, B), (B, T_2), (T_2, C), (C, T_3), (T_3, D), (D, T_4), (T_4, E), (E, T_3), (T_5, A), (T_5, B), (R, T_1), (S, T_1), (S, T_2), (T, T_3), (T, T_4), (T_3, R), (T_5, S), (T_5, T)\}$

The **node** function maps each arc into a pair where the first element is the source node and the second the destination node. In the example:

- $N((A,T_1)) = (\text{source}, \text{dest})$.
- $N((T_1,B)) = (\text{dest}, \text{source})$.

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**Figure 1.** Example of Typestate Oriented Programming in PLAID.

**Figure 2.** Place/Transition Nets.
The colour function $C$ maps each place $p$, to a colour set $C(p)$. In the example:

- if $p \in \{A, B, C, D, E\}$ then $C(p) = P$, otherwise $C(p) = E$.

The guard function $G$ maps each transition $t$ to an expression of type boolean ($Type(G(t)) = Boolean$) i.e. a predicate. Moreover, all variable in $G(t)$ must have types that belongs to $\Sigma$, (that is to say $Type(Var(G(t)))$). In the example:

- $G(t) = [x = q]$ if $t = T1$, otherwise $G(t) = true$.

The arc expression function $E$ maps each arc into an expression which must be of the type $C(p(a))_{Bag}$. In the example:

- $E(a) = 2$ if $a \in \{(R, T1), (S, T1), (T, T4)\}$.
- $E(a) = 2e$ if $a = (T5, S)$.
- $E(a) = case x of p \Rightarrow 2e|q \Rightarrow 1'e$ if $a \in \{(S, T2), (T5, T)\}$
- $E(a) = if x = q then 1'e$ else empty if $a = (T3, R)$
- $E(a) = if x = p$ then $1'e$ else empty if $a = (T, T3)$
- $E(a) = if x = q$ then $1'(q, i + 1)$ else empty if $a = (T5, A)$
- $E(a) = if x = p$ then $1'(p, i + 1)$ else empty if $a = (T5, B)$
- $E(a) = x, i$ otherwise

The initialization function $I$ maps each place $p$ into a expression which must be of type $C(p)_{Bag}$. In the example:

- $I(p) = S'(q, 0)$ if $p = A$
The markings $M_0$ and $M_2$ is directly reachable from $M_0$ (see the figure).

It is possible that two transitions in a CP-net can be concurrently enabled. In the example:

- $T_1', < x = q, i = 0 > + 1'(T_2, < x = p, i = 0 >)$

### 3.4 Benefits and advantages of CP-nets

Some benefits [7]) of CP-nets are:

- Graphical representation
- Well-defined semantics
- Generality
- Few, but powerful primitives
- Explicit description of states and actions
- Hierarchical descriptions
- Computer tools supporting their drawing, simulation and analysis.

### 4. Typestate-Oriented Design: Coloured Petri Nets

This section shows the use of CP-nets as design tool for typestate programming. The procedure for using CP-nets is as follows:

- The places are the typestates.
- The transitions are the methods that makes typestate change.
- The colour set determine the types handled by the CP-net.
- The guards specifies some conditions for change the typestates.
- The arcs determine the data values.
- The tokens carries the data value that belongs to the type associated with the place.
- The initial marking is the starting point for the CPN-net operation.

The CPN-net approach (Figure 10, Figure 14, Figure 15) is more concise than the state machine described (Figure 9, Figure 13).

I show the use of a CPN-net through a series of examples (all examples was taken from the article Typestate-oriented programming [1]). Examples were modeled with CPNTOOLS [11] software.

### 4.1 Example: Iterators

This example shows a iterator. The Iterator state has two states: avail and end. Figure 7 shows the source code in Plaid. Figure 8 shows how a client may use an iterator in Plaid. Figure 9 shows a iterator state machine. The figure 10 shows the CPN-net approach.

- Places. (Avail, End)
- Transitions. (next())
state Iterator {
    conserved type TElem;
    final immutable Collection<TElem> coll;
}

state Avail extends Iterator {
    TElem next() [Avail >> (Avail || End)];
}

state End extends Iterator {
}

Figure 7. Iterators in Plaid.

Collection<String> c = ... Iterator<String> i = c.iterator();

while(i instate Avail) {
    String o = i.next();
}

Figure 8. Iterator client code in Plaid.

Figure 9. Iterator State Machine.

- Colour set. (Element)
- Guards. (n > 1, n = 1)
- Arcs. (empty, e)
- Tokens. (ne)
- Initial marking. (10,e)

4.2 Example: Graphical Interface

This example shows a graphical interface with two states: idle and running. Figure 11 shows the source code in Plaid. Figure 12 shows how a client may use an iterator in Plaid. Figure 13 shows an iterator state machine.

The figure 13 shows the CPN-net approach.

- Places. (Running, Idle)
- Transitions. (start() and stop())
- Colour set. (Element)
- Guards. (null)
- Arcs. (e)
- Tokens. (1e)
- Initial marking. (1’e)

state Idle {
    void start() [Idle >> Running];
}

state Running {
    void stop() [Running >> Idle];
    void run(InputEvent e);
}

Figure 10. Iterator with CPN-net.

state MoveIdle extends Idle {
    GraphicalObject go;
    void start() [Idle >> Running] {
        this <= Running {
            void run(InputEvent e) {
                go.move(e.x,e.y);
            }
            void stop() [Running >> Idle] {
                this <= MoveIdle()
            }
        }
    }
}

Figure 11. Graphical interface code in Plaid.

Figure 12. Graphical interface client code in Plaid.

Figure 13. Graphical interface state machine.
4.3 Example: Files

This example shows a File with two states: OpenFile and ClosedFile. Figure 1 shows the source code in Plaid.

The figure 15 shows the CPN-net approach.

- Places. (OpenFile, ClosedFile)
- Transitions. (read(), open() and closed())
- Colour set. (File, Data, INF)
- Guards. (ptrFile<>null, data<>vacio)
- Arcs. (1ptrFile)
- Tokens. (1ptrFile, 1'(ptrFile, data))
- Initial marking. (1ptrFile + 1'(ptrFile, data))

5. Conclusions

CPN-nets have a well-defined semantics which unambiguously defines the behavior of each CPN-net. CPN-nets are very general and can be used to describe a range from informal systems to formal systems. For this reason, CPN-nets are suitable for modelling typestates. CPN-nets have a number of formal analysis methods (not described in this paper) by which properties of CPN-nets can be proved.

Typestate programming is a new programming paradigm that is actually developed in Carnegie Mellon University. Plaid (currently developing) is a language for Typestate programming. I show that CPN-nets can be used in successfully manner for design typestates.

References


